

CORRIGENDUM

Nonlinear evolution of interacting oblique waves on
 two-dimensional shear layers

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There should be minus signs in front of the right-hand sides of (3.34), (3.39), (3.56), and (3.61), and minus signs preceding the 2 and the 4 in the square brackets on the right-hand side of (3.42) should be changed to pluses. There should be a factor of 2 multiplying the right side of (3.47), the second term on the right-hand side of (3.59) should be replaced by its complex conjugate, and the first minus sign on the right-hand side of (3.60) should be a plus. This changes the kernel function (3.67) to

$$\begin{aligned} K(\bar{x}|\tilde{x}, \tilde{x}_1) &= -\frac{1-2\sin^2\theta}{2}(\bar{x}-\tilde{x})\{(\bar{x}-\tilde{x})[2(\bar{x}-\tilde{x})+(\tilde{x}-\tilde{x}_1)] \\ &\quad +2\sin^2\theta(\bar{x}-\tilde{x}_1)(\tilde{x}-\tilde{x}_1)\} \\ &= -\frac{1}{2}\cos 2\theta(\bar{x}-\tilde{x})[(\bar{x}-\tilde{x})^2+(\bar{x}-\tilde{x}_1)^2-\cos 2\theta(\bar{x}-\tilde{x}_1)(\tilde{x}-\tilde{x}_1)]. \end{aligned}$$

The \bar{X} in the equation preceding (3.32) should be lower case, and there should be an asterisk on the third A in the integrand of the right-hand side of (3.66). Then (4.3) becomes

$$\begin{aligned} D(\sigma) &= -\frac{1}{2}\cos 2\theta \int_1^\infty \frac{1}{v^{3+i\sigma}} \int_v^\infty \frac{du dv}{u^{3+i\sigma}(u+v-1)^{3-i\sigma}} (v-1) \\ &\quad \times \{(v-1)^2+(u-1)^2-\cos 2\theta(u-1)(u-v)\} \\ &= -\frac{1}{2}\cos 2\theta \int_1^\infty \frac{1}{v^{3+i\sigma}(v-1)^2} \left\{ \sum_{m=-2}^2 \frac{\hat{C}_m(v|\theta)}{m+i\sigma} \left[\left(\frac{2v-1}{v} \right)^{m+i\sigma} - 1 \right] \right\} dv \\ &= -\frac{1}{2}\cos 2\theta \int_0^1 \frac{(1-x)^{3+i\sigma}}{x^4} \left\{ \sum_{m=-2}^2 \frac{\tilde{C}_m(x|\theta)}{m+i\sigma} [(1+x)^{m+i\sigma} - 1] \right\} dx, \end{aligned}$$

and the formulae for the C are given in the revised Appendix. This changes the final results, which are plotted in the revised figures 1–5 (figures C1–C5). Introducing the rescaled variables $\bar{A} \equiv A\bar{\kappa}_r^6/|\gamma\bar{\kappa}|$ and $\bar{x}_1 \equiv \bar{\kappa}_r\bar{x}-x_0$ into (3.69), where $\bar{\kappa}_r \equiv \text{Re } \bar{\kappa}$, and properly choosing x_0 and X_0 in (3.25) and (3.27) shows that $\bar{A}e^{-\bar{x}\bar{x}}$ is a function of \bar{x}_1 and the single parameter $\arg \bar{\kappa}\gamma$. We therefore plot the results in terms of these more universal variables, rather than those of the original paper. This reduces the number of figures, which are now drawn for $\theta = \frac{1}{8}\pi$, since the corrected kernel function vanishes at $\theta = \frac{1}{4}\pi$.

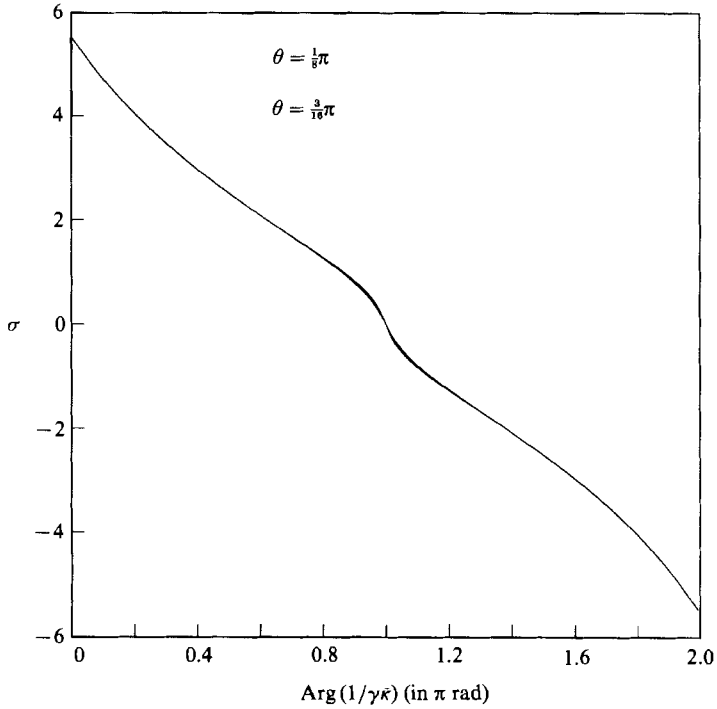


FIGURE C1. Asymptotic exponent σ vs. $\text{Arg}(1/\gamma\bar{\kappa})$ in π radians.

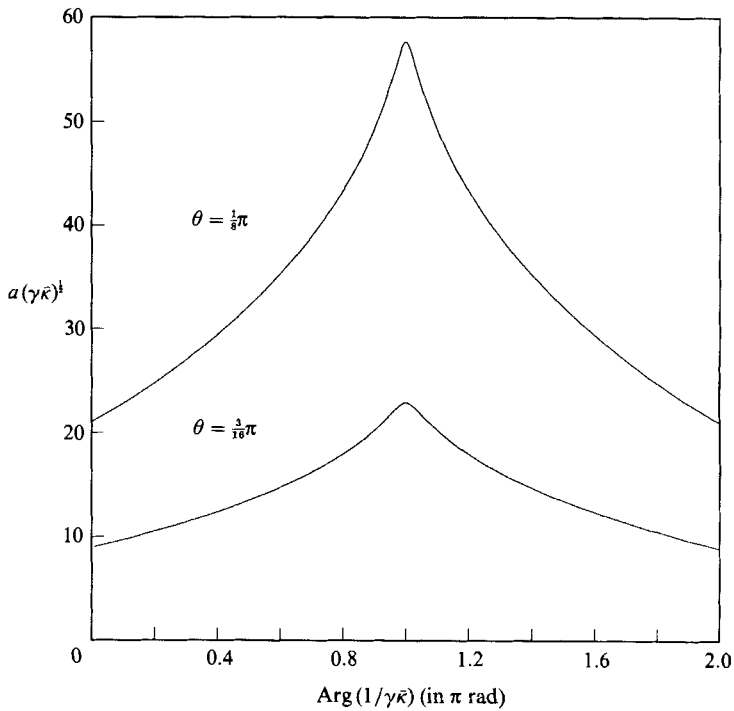


FIGURE C2. Normalized asymptotic amplitude $a(\gamma\bar{\kappa})^{1/2}$ vs. $\text{Arg}(1/\gamma\bar{\kappa})$ in π radians.

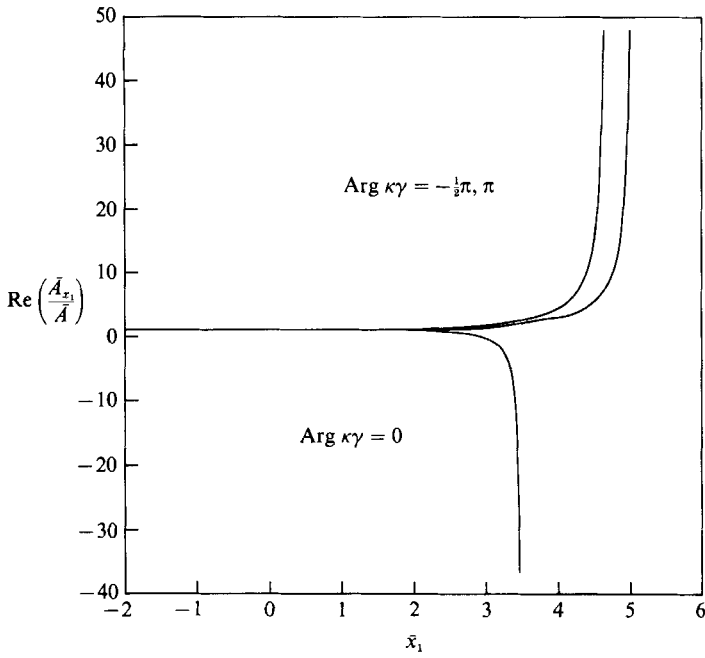


FIGURE C3. Scaled growth rate $\text{Re}(\bar{A}_{x_1}/\bar{A})$ vs. scaled streamwise coordinate \bar{x}_1 for $\theta = \frac{1}{3}\pi$.

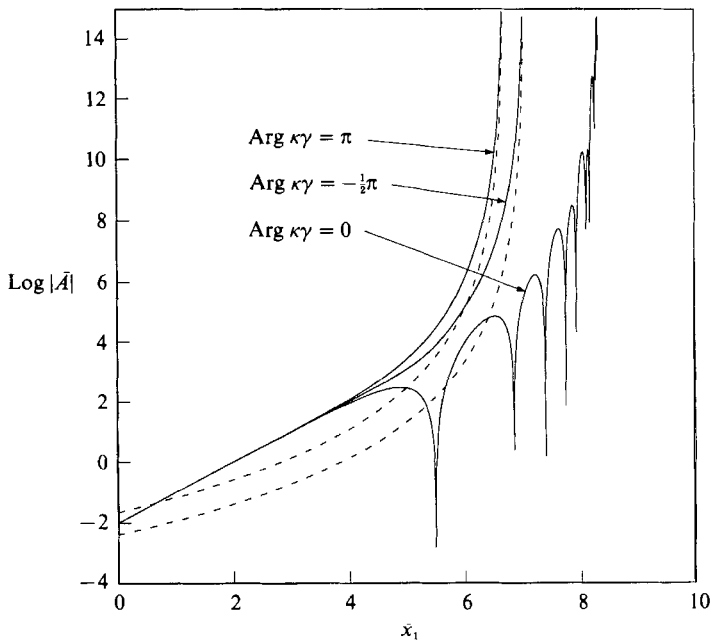


FIGURE C4. Scaled amplitude $\log |\bar{A}|$ vs. scaled streamwise coordinate \bar{x}_1 for $\theta = \frac{1}{3}\pi$.

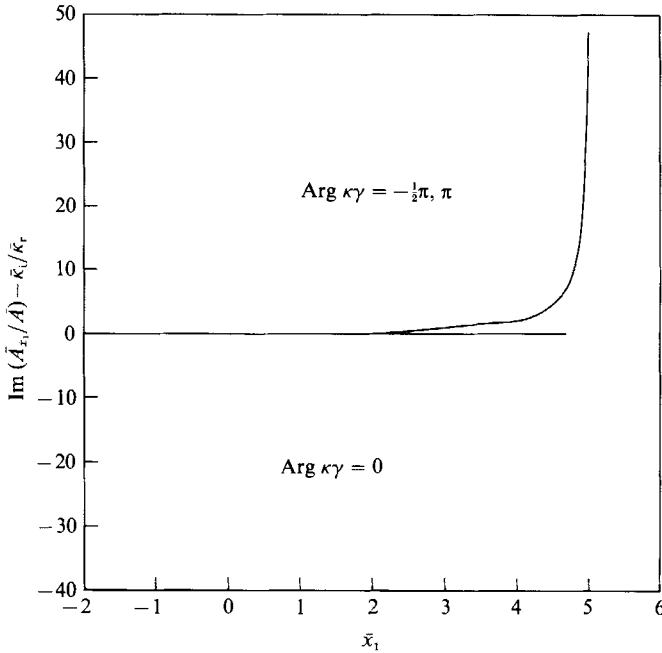


FIGURE C5. Phase $\text{Im}(\bar{A}_{x_1}/\bar{A})$ vs. scaled streamwise coordinate \bar{x}_1 for $\theta = \frac{1}{8}\pi$.

Appendix

The detailed expressions for coefficients used in the revised equation (4.3) and (4.4) are

$$\hat{C}_2 = \frac{2-v}{v-1} - \frac{2v}{(v-1)^2} \sin^2 \theta, \tag{A 1}$$

$$\hat{C}_1 = \frac{3v-7}{v-1} + \frac{2(v^2+4v-1)}{(v-1)^2} \sin^2 \theta, \tag{A 2}$$

$$\hat{C}_0 = \frac{9-3v}{v-1} - \frac{2(4v^2+4v-2)}{(v-1)^2} \sin^2 \theta, \tag{A 3}$$

$$\hat{C}_{-1} = \frac{v-5}{v-1} + \frac{2(5v^2-1)}{(v-1)^2} \sin^2 \theta, \tag{A 4}$$

$$\hat{C}_{-2} = \frac{1}{v-1} - \frac{2(2v^2-v)}{(v-1)^2} \sin^2 \theta, \tag{A 5}$$

$$\tilde{C}_2 = -(2x^2 - 2x + 1) - (x - 1) \cos 2\theta, \tag{A 6}$$

$$\tilde{C}_1 = 2(3x^2 - 3x + 2) + (x^2 + 2x - 4) \cos 2\theta, \tag{A 7}$$

$$\tilde{C}_0 = -(7x^2 - 6x + 6) - 2(x^2 - 3) \cos 2\theta, \tag{A 8}$$

$$\tilde{C}_{-1} = 2(2x^2 - x + 2) + (x^2 - 2x - 4) \cos 2\theta, \tag{A 9}$$

$$\tilde{C}_{-2} = (x^2 + 1) + (x + 1) \cos 2\theta, \tag{A 10}$$

$$C_{1,2} = (-1 - i\sigma)_{n+2} - 4(-i\sigma)_{n+2} + 6(1 - i\sigma)_{n+2} - 4(2 - i\sigma)_{n+2} + (3 - i\sigma)_{n+2}, \tag{A 11}$$

$$C_{2,2} = -2(-1 - i\sigma)_{n+2} + 6(-i\sigma)_{n+2} - 6(1 - i\sigma)_{n+2} + 2(2 - i\sigma)_{n+2}, \quad (\text{A } 12)$$

$$C_{3,2} = 2(-1 - i\sigma)_{n+2} - 6(-i\sigma)_{n+2} + 7(1 - i\sigma)_{n+2} - 4(2 - i\sigma)_{n+2} + (3 - i\sigma)_{n+2}, \quad (\text{A } 13)$$

$$2C_{1,0} = 2C_{1,4} = -(-1 - i\sigma)_{n+2} + 4(-i\sigma)_{n+2} - 6(1 - i\sigma)_{n+2} + 4(2 - i\sigma)_{n+2} - (3 - i\sigma)_{n+2}, \quad (\text{A } 14)$$

$$2C_{2,0} = 2C_{2,4} = (-1 - i\sigma)_{n+2} - 2(-i\sigma)_{n+2} + 2(2 - i\sigma)_{n+2} - (3 - i\sigma)_{n+2}, \quad (\text{A } 15)$$

$$2C_{3,0} = 2C_{3,4} = -(-i\sigma)_{n+2} + 2(1 - i\sigma)_{n+2} - (2 - i\sigma)_{n+2}, \quad (\text{A } 16)$$